A Curved Spiral Antenna Above a Conducting Cylinder

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Abstract—A curved spiral antenna above a finite hollow conducting cylinder is analyzed using the method of moments. The effects of cylinder length $2H$ and cylinder radius r_{cy} on the radiation characteristics of the spiral are evaluated. As $2H$ increases, the cross-polarization component of the radiation field in the broadside direction decreases to a constant value (approximately -18 dB). When $2H$ is greater than one wavelength (λ_0), the input impedance of the spiral above a cylinder of radius $r_{cy} = 0.25\lambda_0$ is almost constant ($250 - j20 \Omega$) with a gain of approximately 7 dB. The spiral above a cylinder of $(2H, r_{cy}) = (2.7\lambda_0, 0.25\lambda_0)$ shows a 3-dB axial ratio bandwidth of approximately 23%, which is wider than a flat spiral antenna above a flat ground plane of infinite extent.

Index Terms—Measurements, moment-method solutions, spiral antenna.

I. INTRODUCTION

A CURVED radiation element mounted above a conducting cylinder has been receiving attention as a mobile communication antenna. Ashkenazy *et al.* [1] have revealed the radiation field from a microstrip antenna above a cylinder using an assumed surface-current distribution on the antenna. Nakatani *et al.* [2] have obtained Green's functions in dyadic form for a dipole printed on a grounded cylindrical substrate. Habashy *et al.* [3] have formulated the current distribution of a patch above a cylinder using a cylindrically stratified medium approach. More recently, Rostan *et al.* [4] have analyzed a microstrip patch array above a cylinder using a sinusoidal current distribution on the resonant patch elements. These antennas radiate a linearly polarized wave and have a conducting cylinder of infinite length.

An antenna having circular polarization (CP) is also useful as a mobile communication antenna [5]. A spiral antenna is a CP radiator and is a candidate for such an application. This paper presents a curved square spiral antenna above a conducting cylinder of *finite length*. It should be emphasized that the surface of the spiral antenna is parallel to the conducting cylinder.

For numerical analysis, the cylinder of finite length is approximated by grid wires [6]. The method of moments [7] is applied to an electric field integral equation [8] to obtain the current distribution on the spiral and cylinder. The radiation characteristics, including the input impedance, radiation pattern, axial ratio, and gain, are evaluated using the obtained current distributions. These radiation characteristics are compared with those of a flat spiral antenna above a flat

Fig. 1. Configuration and coordinate system.

conducting plate (reflector). This flat spiral is used as the reference antenna throughout this paper.

Attention is paid to investigating the effects of the cylinder length and radius on the radiation characteristics of the curved spiral. The radiation characteristics as a function of cylinder length are calculated for a fixed cylinder radius of $r_{cy} = 0.25\lambda_0$, where λ_0 is the wavelength at a test frequency of 3 GHz. In addition, the radiation characteristics as a function of cylinder radius are calculated for a fixed cylinder length of $2H = 2.7\lambda_0$. Based on these investigations, the frequency responses of the input impedance, axial ratio, and gain of a curved spiral antenna above a cylinder of $(2H, r_{cy}) = (2.7\lambda_0, 0.25\lambda_0)$ are analyzed. It is found that the curved spiral has a bandwidth of approximately 23% for a 3-dB axial ratio criterion.

Some experiments for the curved spiral are performed to confirm the validity of the theoretical results. It is found that good agreement between experimental and theoretical results is obtained.

II. CONFIGURATION

Fig. 1 shows the configuration and coordinate system of a curved square spiral antenna above a finite hollow cylinder whose length is designated as $2H$. Note that the hollow

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cylinder does not have any end caps. The spiral is located at height $h = r_{sp} - r_{cy}$, where r_{sp} is the radius of the surface of the curved spiral and r_{cy} is the radius of the conducting cylinder. The conducting cylinder acts as a reflector for the curved spiral.

The spiral, which is supported by air honeycomb of relative permittivity $\epsilon_r = 1$, is excited by a voltage source at the spiral center. Throughout this paper, the following configuration parameters are fixed: wire radius of the spiral $\rho = 0.3 \text{ mm} = 0.003\lambda_0$, antenna height $h = 20 \text{ mm} = 0.2\lambda_0$, and filament lengths of the spiral $\ell_n = 2\ell_1(n-1)$ for $n = 2, 3, 4, \dots, 10$ with a start filament length of $\ell_1 = 1.7 \text{ mm} = 0.017\lambda_0$ and an end filament length of $\ell_{11} = 30.8 \text{ mm} = 0.308\lambda_0$. The cylinder radius r_{cy} , the spiral radius r_{sp} , and the cylinder length $2H$ are varied subject to the objectives of the analysis.

A flat spiral antenna ($r_{sp} = \infty$) with the above-mentioned configuration parameters, backed by a flat conducting reflector of infinite extent ($r_{cy} = \infty$, $2H = \infty$), radiates a circularly polarized wave with an axial ratio of 1.4 dB. (Note that the height ($r_{sp} - r_{cy}$) is held constant while r_{sp} and r_{cy} tend to infinity, and this height is the same as that for the finite-radius cylinder case.) This flat spiral is used as the reference antenna in this paper.

III. NUMERICAL RESULTS

The cylinder is approximated by grid wires, which are uniformly spaced in the vertical and circumferential directions. The currents along the spiral and cylinder are obtained using the method of moments in which piecewise sinusoidal expansion and weighting functions [8] are used. The radiation characteristics, including the input impedance, radiation pattern, axial ratio, and gain, are evaluated on the basis of the obtained current distribution. Throughout this paper the axial ratio is always evaluated on the z axis (broadside).

A preliminary investigation shows that the gain converges as the grid-wire spacing decreases. From the convergence test of the gain, a grid-wire space of approximately $0.06\lambda_0$ is used in the following analysis [9]. Note that the radius of the grid wires is chosen to be the same as that of the spiral arm wire ($0.003\lambda_0$).

A. Effects of Cylinder Length $2H$

First, we investigate the effects of the cylinder length $2H$ on the radiation characteristics, fixing the cylinder radius to be one-quarter wavelength ($r_{cy} = 0.25\lambda_0$) with a spiral radius of $r_{sp} = r_{cy} + h = 0.25\lambda_0 + 0.2\lambda_0$.

Fig. 2 shows the input impedance $Z_{in} = R_{in} + jX_{in}$ as a function of the cylinder length $2H$. It is found that the input impedance is almost constant when the cylinder length is greater than one wavelength (λ_0). The resistance value is approximately 250Ω with a reactance value of approximately -20Ω .

The behavior of the input impedance is related to the current distribution along the spiral arms. Fig. 3 shows the current distribution $I = I_r + jI_i$ for $2H = 2.7\lambda_0$. Detailed calculations reveal that the spiral has a gradually decaying traveling-wave current with an almost constant value at the feed point when

Fig. 2. Input impedance as a function of cylinder length $2H$. $r_{cy} = 0.25\lambda_0$, $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$.

Fig. 3. Current distribution on spiral arms. $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$, PP: phase progression - - -, FSPP: free-space phase progression —.

the cylinder length $2H$ is greater than λ_0 . This leads to a constant input impedance.

Regarding the current distribution on the cylinder, the current (amplitude $|I|$) along the longitudinal grid wire at $(x, y, z) = (0, y, 0.25\lambda_0)$ (one of the grid wires modeling the cylinder) is shown in Fig. 4, where the cylinder length $2H$ ranges from $0.6\lambda_0$ to $4.7\lambda_0$. The arrows (from $y = -0.15\lambda_0$ to $y = +0.15\lambda_0$) on the cylinder illustrate the projection of the spiral into the cylinder surface. It is found that the induced current on the cylinder is concentrated under the spiral.

The radiation field is obtained as the superposition of the radiation due to the current along the spiral arms and the radiation due to the current induced along the cylinder. Fig. 5 shows the radiation patterns for different cylinder lengths. E_R and E_L in this figure are the right- and left-hand circularly polarized wave components, respectively.

As seen from Fig. 5, the cross-polarization component (E_L) in the $+z$ direction decreases as the cylinder length $2H$ increases. The cross-polarization component is approximately -18 dB when $2H > 2\lambda_0$. It is also found that as the cylinder length increases, the ratio of the front lobe to the back lobe (FB ratio) of the copolarization component E_R improves. The FB ratio is approximately 15 dB when $2H > 2\lambda_0$. The experimental results at a test frequency $f_0 = 3 \text{ GHz}$

Fig. 4. Current distribution along the longitudinal grid wire at $(x, y, z) = (0, y, 0.25\lambda_0)$, one of the grid wires modeling the cylinder with $r_{cy} = 0.25\lambda_0$ and $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$. (a) $2H = 0.6\lambda_0$. (b) $2H = 2.3\lambda_0$. (c) $2H = 4.7\lambda_0$.

are also presented in Fig. 5(c), showing good agreement with theoretical results.

From the abovementioned current distribution, input impedance, and radiation pattern, we can see that the gain and axial ratio exhibit almost constant values for $2H > 2\lambda_0$. Fig. 6 shows the gain and axial ratio as a function of cylinder length $2H$. A gain of approximately 7 dB is obtained for $2H > 2\lambda_0$. This gain is smaller than the gain of the reference antenna ($G_{\text{ref}} = 8.7$ dB) due to the radiation toward the rear region ($-z$ region). The axial ratio for $2H > 2\lambda_0$ is close to that of the reference antenna ($AR_{\text{ref}} = 1.4$ dB).

B. Effects of Cylinder Radius r_{cy}

We consider the effects of the cylinder radius r_{cy} on the radiation characteristics. For this, the cylinder length $2H$ is chosen to be long enough not to affect the radiation characteristics. Taking into account the results of the previous section, we fix the cylinder length $2H$ to be greater than two wavelengths: $2H = 2.7\lambda_0$.

The cylinder radius r_{cy} is varied while maintaining the antenna height h constant. The spiral radius r_{sp} is also varied: $r_{sp} = r_{cy} + h = r_{cy} + 0.2\lambda_0$. Fig. 7 shows the input impedance of the curved spiral as a function of the cylinder radius r_{cy} . The theoretical values of resistance and reactance for the reference antenna are also presented on the right-hand vertical axis. Note that the input impedance for $r_{cy} > 0.8\lambda_0$ is nearly equal to that of the reference antenna. For confirmation, experiments are performed at $f_0 = 3$ GHz. The antenna for the experiments is fed from a coaxial line with a balun circuit. The theoretical and experimental results are in good agreement.

The theoretical gain and axial ratio of the curved spiral are shown as a function of r_{cy} in Fig. 8, together with experimental results. The black and white dots on the right indicate the theoretical gain (G_{ref}) and axial ratio (AR_{ref})

Fig. 5. Radiation pattern as a function of cylinder length $2H$. $r_{cy} = 0.25\lambda_0$, $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$. E_R { theoretical —, experimental ••• }, E_L { theoretical ---, experimental ○○••• }. (a) $2H = 0.3\lambda_0$. (b) $2H = 1.0\lambda_0$. (c) $2H = 2.7\lambda_0$. (d) $2H = 5.0\lambda_0$.

Fig. 6. Gain and axial ratio as a function of cylinder length $2H$. $r_{cy} = 0.25\lambda_0$, $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$.

for the reference antenna, respectively. The radiation from the curved spiral is circularly polarized with an axial ratio of less than 3 dB for $r_{cy} > 0.2\lambda_0$. The value of the axial ratio

Fig. 7. Input impedance as a function of cylinder radius r_{cy} . $r_{sp} = r_{cy} + 0.2\lambda_0$, $2H = 2.7\lambda_0$, R_{in} { theoretical —, experimental ■ ■ }, X_{in} { theoretical ---, experimental □ □ }, reference antenna theoretical { R_{in} —, X_{in} --- }.

Fig. 8. Gain and axial ratio as a function of cylinder radius r_{cy} . $r_{sp} = r_{cy} + 0.2\lambda_0$, $2H = 2.7\lambda_0$, gain { theoretical ---, experimental ■ ■ }, axial ratio { theoretical —, experimental □ □ }, reference antenna theoretical { gain —, axial ratio --- }.

at $r_{cy} = 0.8\lambda_0$ is almost the same as that of the reference antenna.

The current (amplitude $|I|$) flowing along the rear half of the cylinder (from $\theta = 90^\circ$ – 270°) decreases as the cylinder radius r_{cy} increases. This is shown in Fig. 9. Note that the current in this figure is calculated for the circumferential grid wire of the cylinder model at $y = 0$. The decrease in the current over a region from $\theta = 90^\circ$ – 270° results in less radiation from the rear region, as shown in Fig. 10, and the copolarization component E_R has a FB ratio of more than 20 dB for $r_{cy} > 0.5\lambda_0$. The theoretical and experimental results are in good agreement in Fig. 10(b) and (d).

C. Frequency Responses

Effects of the cylinder length $2H$ and the cylinder radius r_{cy} on the radiation characteristics at a frequency $f_0 = 3$ GHz were discussed in Section III-A and B. In this section, we reveal the frequency response of the radiation characteristics.

The cylinder radius r_{cy} for the curved spiral antenna is chosen to be small in order to clarify the difference in the frequency responses between the curved and reference antennas: $r_{cy} = 0.25\lambda_0$ with cylinder length $2H = 2.7\lambda_0$,

Fig. 9. Current distribution along the wire at $y = 0$, which is one of the circumferential grid wires modeling the cylinder with $r_{sp} = r_{cy} + 0.2\lambda_0$ and $2H = 2.7\lambda_0$.

Fig. 10. Radiation pattern as a function of cylinder radius r_{cy} . $r_{sp} = r_{cy} + 0.2\lambda_0$, $2H = 2.7\lambda_0$, E_R { theoretical —, experimental ● ● }, E_L { theoretical ---, experimental ○ ○ }. (a) $r_{cy} = 0.05\lambda_0$. (b) $r_{cy} = 0.5\lambda_0$. (c) $r_{cy} = 0.8\lambda_0$. (d) $r_{cy} = \infty$ (reference antenna).

where λ_0 is the wavelength at the frequency $f_0 = 3$ GHz. The solid lines in Fig. 11 show the frequency response of the input impedance for the curved spiral. The resistance and reactance

Fig. 11. Frequency response of input impedance. $r_{cy} = 0.25\lambda_0$, $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$, $2H = 2.7\lambda_0$,
 curved spiral antenna { theoretical — experimental • •
 reference antenna theoretical - - -.

Fig. 12. Frequency response of axial ratio. $r_{cy} = 0.25\lambda_0$, $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$, $2H = 2.7\lambda_0$,
 curved spiral antenna { theoretical — experimental • •
 reference antenna theoretical - - -.

values for the reference antenna are shown by dashed lines. It is found that the difference in the impedance between the two antennas is not significant at frequencies higher than f_0 . The curved and reference spirals have an almost pure resistance of 250Ω . Note that the black dots show the experimental results for the curved spiral.

Fig. 12 shows the frequency response of the axial ratio. The curved spiral has a wider 3-dB axial ratio bandwidth than the reference antenna: 23% for the curved spiral and 15% for the reference antenna. Over these frequency bandwidths, the gains for the curved spiral and reference antenna show almost constant values (as shown in Fig. 13): approximately 7 dB for the curved spiral and approximately 8 dB for the reference antenna. The experimental results for the curved spiral are presented in Figs. 12 and 13, showing good agreement with theoretical results.

Based on the above results, it can be said that the curved spiral has wide-band performance comparable to that of the reference antenna.

IV. CONCLUSIONS

A curved spiral antenna above a conducting cylinder of *finite* length is analyzed using the method of moments. A flat spiral antenna backed by a flat reflector of infinite extent is also analyzed as a reference antenna.

Fig. 13. Frequency response of gain. $r_{cy} = 0.25\lambda_0$, $r_{sp} = 0.25\lambda_0 + 0.2\lambda_0$, $2H = 2.7\lambda_0$,
 curved spiral antenna { theoretical — experimental • •
 reference antenna theoretical - - -.

First, the effects of cylinder length $2H$ on the radiation characteristics are evaluated for a fixed cylinder radius of $r_{cy} = 0.25\lambda_0$. It is found that the curved spiral antenna has a constant input impedance ($250 - j20 \Omega$) for cylinder length $2H > \lambda_0$ due to a constant traveling-wave current distribution along the spiral arms. As the cylinder length $2H$ increases, the cross-polarization component in the broadside direction decreases to a constant value (approximately -18 dB) and the FB ratio improves. The gain of the curved spiral is calculated to be approximately 7 dB for $2H > 2\lambda_0$, which is slightly lower than the gain of the reference antenna ($G_{ref} = 8.7$ dB).

Second, the effects of the cylinder radius r_{cy} on the radiation characteristics are investigated using a curved spiral antenna with a fixed cylinder length of $2H = 2.7\lambda_0$. When $r_{cy} > 0.8\lambda_0$, the input impedance and the axial ratio are nearly equal to those of the reference antenna. The copolarization component of the radiation field has a FB ratio of more than 20 dB for $r_{cy} > 0.5\lambda_0$.

Finally, the frequency responses of the radiation characteristics are revealed for a cylinder of $(2H, r_{cy}) = (2.7\lambda_0, 0.25\lambda_0)$. The curved spiral has a frequency bandwidth of 23% for a 3-dB axial ratio criterion, which is wider than the reference antenna (15%). It is also found that the gain of the curved spiral is approximately 7 dB over this 23% frequency bandwidth.

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